## DRAFT

## Algebra 2 EOC Item Specifications

The draft Florida Standards Assessment (FSA) Test Item Specifications (Specifications) are based upon the Florida Standards and the Florida Course Descriptions as provided in CPALMs. The Specifications are a resource that defines the content and format of the test and test items for item writers and reviewers. Each grade-level and course Specifications document indicates the alignment of items with the Florida Standards. It also serves to provide all stakeholders with information about the scope and function of the FSA.

Item Specifications Definitions

Also assesses refers to standard(s) closely related to the primary standard statement.

Clarification statements explain what students are expected to do when responding to the question.

Assessment limits define the range of content knowledge and degree of difficulty that should be assessed in the assessment items for the standard.

Acceptable response mechanisms describe the characteristics from which a student must answer a question.

Context defines types of stimulus materials that can be used in the assessment items.

Algebra 2 EOC Item Specifications
Florida Standards Assessments

| MAFS.912.A-APR.1.1 <br> Also assesses <br> MAFS.912.A-APR.3.4 | Understand that polynomials form a system analogous to the integers; namely, they are closed under the operations of addition, subtraction, and multiplication; add, subtract, and multiply polynomials. <br> Prove polynomial identities and use them to describe numerical relationships. For example, the polynomial identity $\left(x^{2}+y^{2}\right)^{2}=\left(x^{2}-y^{2}\right)^{2}+$ $(2 x y)^{2}$ can be used to generate Pythagorean triples. |
| :---: | :---: |
| Item Types | Drag and drop response - May require using graphics in the construction of a proof. <br> Equation response - May require creating a value or an expression. <br> Hot spot response - May require identifying steps in the construction of a proof. <br> Movable text response - May require ordering steps in a proof. <br> Multiple-choice response - May require selecting a value, an expression, or a statement from a list. <br> Natural Language response - May require explaining the steps used in generating a polynomial identity. <br> Selectable text response - May require highlighting a step in an informal argument. |
| Clarifications | Students will apply their understanding of closure to adding, subtracting, and multiplying polynomials with rational coefficients. <br> Students will use polynomial identities to describe numerical relationships. <br> Students will use the structure of algebra to complete an algebraic proof of a polynomial identity. |
| Assessment Limits | Items set in a real-world context should not result in a nonreal answer if the polynomial is solved. <br> In items that require addition and subtraction, polynomials are limited to polynomials with no more than 5 terms. The simplified polynomial should contain no more than 8 terms. <br> In items that require multiplication of polynomials, the factors are limited to a product of: two binomials; a monomial and two binomials; a monomial, a binomial, and a trinomial; two trinomials; and a binomial and a polynomial with four terms. The simplified product should contain no more than 9 terms. <br> Polynomial identities are restricted to trinomials, difference of squares, sum of cubes, and difference of cubes. |
| Stimulus Attributes | Items can be set in a mathematical or real-world context. Items can use function notation. |
| Response Attributes | Items may require students to recognize equivalent expressions. Items may require students to rewrite expressions with negative exponents, but items must not require the student to rewrite rational expression as seen in the standard MAFS.912.A-APR.4.6. |
| Calculator | No |

$\left.\begin{array}{|l|l|}\hline \text { MAFS.912.A-APR.4.6 } & \begin{array}{l}\text { Rewrite simple rational expressions in different forms; write } \mathrm{a}(\mathrm{x}) / \mathrm{b}(\mathrm{x}) \text { in } \\ \text { the form } \mathrm{q}(\mathrm{x})+\mathrm{r}(\mathrm{x}) / \mathrm{b}(\mathrm{x}) \text {, where } \mathrm{a}(\mathrm{x}), \mathrm{b}(\mathrm{x}), \mathrm{q}(\mathrm{x}) \text {, and } \mathrm{r}(\mathrm{x}) \text { are polynomials } \\ \text { with the degree of } \mathrm{r}(\mathrm{x}) \text { less than the degree of } \mathrm{b}(\mathrm{x}) \text {, using inspection, } \\ \text { long division, or, for the more complicated examples, a computer } \\ \text { algebra system. } \\ \text { MAFS.912.A-APR.2.2 } \\ \text { Know and apply the Remainder Theorem: For a polynomial } \mathrm{p}(\mathrm{x}) \text { and a } \\ \text { number a, the remainder on division by } \mathrm{x}-\mathrm{a} \text { is } \mathrm{p}(\mathrm{a}) \text {, so } \mathrm{p}(\mathrm{a})=0 \text { if and } \\ \text { only if }(\mathrm{x}-\mathrm{a}) \text { is a factor of } \mathrm{p}(\mathrm{x}) .\end{array} \\ \hline \text { Item Types } & \begin{array}{l}\text { Drag and drop response - May require using completing long division. } \\ \text { Equation response - May require creating an expression or a value. } \\ \text { Graphic response - May require graphing the location of key features. } \\ \text { Multiple-choice response - May require identifying an expression or a } \\ \text { value. } \\ \text { Multi-select response - May require choosing factors from a list. } \\ \text { Natural Language response - May require explaining what a value } \\ \text { means. }\end{array} \\ \hline \text { Clarifications } & \begin{array}{l}\text { Students will rewrite a rational expression as the quotient in the form of } \\ \text { a polynomial added to the remainder divided by the divisor. } \\ \text { Students will use polynomial long division to divide a polynomial by a } \\ \text { polynomial. } \\ \text { Students will use the Remainder Theorem to determine if }(\mathrm{x}-\mathrm{a}) \text { is a } \\ \text { factor. } \\ \text { Students will use the Remainder Theorem to determine the remainder of } \\ \mathrm{p}(\mathrm{x}) /(\mathrm{x}-\mathrm{a}) .\end{array} \\ \hline \text { Assessment Limits } & \begin{array}{l}\text { The polynomial that is the dividend should have a degree no less than 3 } \\ \text { and no greater than } 6 .\end{array} \\ \text { The polynomial that is the divisor should have a degree of 1, 2, or 3. }\end{array}\right\}$

Algebra 2 EOC Item Specifications
Florida Standards Assessments

| Stimulus Attributes | Items should be set in a mathematical context. |
| :--- | :--- |
|  | Items can use function notation. |
| Response Attribute | Items may require the student to provide sub-steps to complete <br> polynomial long division. |
| Calculator | No |

Algebra 2 EOC Item Specifications
Florida Standards Assessments

| MAFS.912.A-CED.1.1 | Create equations and inequalities in one variable and use them to solve <br> problems. Include equations arising from linear and quadratic functions and simple <br> rational, absolute, and exponential functions. <br> Solve simple rational and radical equations in one variable, and give <br> examples showing how extraneous solutions may arise. |
| :--- | :--- |
| MAFS.912.A-REI.1.2 |  |
| Also assesses |  |
| MAFS.912.A-CED.1.4 | Rearrange formulas to highlight a quantity of interest using the same <br> reasoning as in solving equations. For example, rearrange Ohm's law, <br> $V=I R, ~ t o ~ b i g h l i g h t ~ r e s i s t a n c e, ~ R . ~$ |
| Item Types | Drag and drop response - May require rearranging equations. <br> Equation response - May require creating an equation, an inequality, or a <br> value. <br> Hot spot response - May require selecting key features of a function. <br> Multiple-choice response - May require identifying an equation or a <br> value from a list of four choices. <br> Natural Language response - May require creating a written explanation. |
| Clarifications | Students will write and solve an equation that represents a real-world <br> context in one variable. <br> Students will solve a rational equation in one variable. <br> Students will solve a radical equation in one variable. <br> Students will justify algebraically why a solution is extraneous. <br> Students will solve multi-variable formulas or literal equations for a <br> specific variable. |


| Assessment Limits | In items that require students to write an equation, equations are limited <br> to simple rational, absolute value, and exponential with rational <br> exponents. <br> Items may include equations that contain variables on both sides. <br> Items that involve formulas should not include overused contexts such <br> as Fahrenheit/Celsius or three-dimensional geometry formulas. <br> In items that require students to solve literal equations and formulas, the <br> term of interest can be quadratic, a cubic in a monomial term, a linear <br> term in the denominator of rational equation, a linear term in a square <br> root equation, or a linear term as the base of an exponential equation <br> with a rational number as the value for the exponent. <br> Items should not require more than four procedural steps to isolate the <br> variable of interest. <br> Items will not assess inequalities. |
| :--- | :--- |
| Stimulus Attributes | Items should be set in a real-world context. <br> Items can use function notation. <br> Items may require the student to choose and interpret units. |
| Response Attribute | Items may require students to recognize equivalent expressions. |
| Calculator | Neutral |

Algebra 2 EOC Item Specifications
Florida Standards Assessments

| MAFS.912.A-CED.1.2 Also assesses | Create equations in two or more variables to represent relationships between quantities; graph equations on coordinate axes with labels and scales. |
| :---: | :---: |
| Also assesses <br> MAFS.912.A-REI.3.6 | Represent constraints by equations or inequalities and by systems of equations and/or inequalities, and interpret solutions as viable or nonviable options in a modeling context. For example, represent inequalities describing nutritional and cost constraints on combinations of different foods. |
| Also assesses <br> MAFS.912.A-REI.3.7 | Solve systems of linear equations exactly and approximately (e.g., with graphs), focusing on pairs of linear equations in two variables. |
|  | Solve a simple system consisting of a linear equation and a quadratic equation in two variables algebraically and graphically. For example, find the points of intersection between the line $y=-3 x$ and the circle $x^{2}+y^{2}=3$. |
| Item Types |  |
|  | Equation response - May require creating an equation, an inequality, or a value. |
|  | Graphic response - May require graphing a representation of an equation or a solution. |
|  | Hot spot response - May require selecting a solution region. Multiple-choice response - May require identifying an equation or a value from a list of four possible choices, identifying graphs, or identifying inequalities. |
|  | Multi-select response - May require identifying equations or inequalities. |
| Clarifications |  |
|  | Students will identify the quantities in a real-world situation that should be represented by distinct variables. |
|  | Students will write a system of equations given a real-world situation. Students will graph a system of equations that represents a real-world |
|  | context using appropriate axis labels and scale. Students will solve systems of linear equations. |
|  | Student will write a system of equations for a modeling context that is best represented by a system of equations. |
|  | Student will write a system of inequalities for a modeling context that is best represented by a system of inequalities. |
|  | Students will interpret the solution of a real-world context as viable or not viable. |
|  | Students will solve a simple system of a linear equation and a quadratic equation in two variables algebraically. |
|  | Students will solve a simple system of a linear equation and a quadratic equation in two variables graphically. |
| Assessment Limits |  |
|  | Items that require a student to write a system of equations using a realworld context are limited to: |
|  | - a system of $2 \times 2$ linear equations with rational coefficients; <br> - a system of $3 \times 3$ linear equations with rational coefficients; |
|  | - a system of two equations with a linear equation with rational coefficients and a quadratic of the form $y=a x^{2}+b x+c$, where a, b, and c are integers; and |

Algebra 2 EOC Item Specifications
Florida Standards Assessments

|  | - a system of two equations with a linear equation with rational coefficients and a quadratic of the form $a x^{2}+b y^{2}=c$, where $a$, b , and c are integers. <br> Items that require a student to graph a system of equations are limited to a $2 \times 2$ system. |
| :---: | :---: |
| Stimulus Attributes | Items can be set in a real-world or mathematical context. Items may result in infinitely many solutions or no solution. |
| Response Attributes | Items may require the student to choose and interpret the scale in a graph. <br> Items may require the student to graph a circle whose center is $(0,0)$. <br> Items may require the student to choose and interpret units. |
| Calculator | Neutral |

Algebra 2 EOC Item Specifications
Florida Standards Assessments

| MAFS.912.A-REI.1.1 | Explain each step in solving a simple equation as following from the <br> equality of numbers asserted at the previous step, starting from the <br> assumption that the original equation has a solution. Construct a viable <br> argument to justify a solution method. |
| :--- | :--- |
| Item Types | Drag and drop response - May require rearranging equations or <br> justifications. <br> Equation response - May require creating an expression. <br> Movable text response - May require ordering steps. <br> Multiple-choice response - May require identifying expressions or <br> statements. <br> Natural Language response - May require creating a written response. <br> Selectable text response - May require highlighting a step in an informal <br> argument. |
| Clarifications | Students will complete an algebraic proof to explain steps for solving a <br> simple equation. <br> Students will construct a viable argument to justify a solution method. |
| Assessment Limit | Items will not require the student to recall names of properties from <br> memory. |
| Stimulus Attributes | Items should be set in a mathematical context. <br> Items can use function notation. <br> Coefficients can be a rational number or a variable that represents any <br> real number. |
| Response Attribute | Items will not ask the student to provide the solution. |

Algebra 2 EOC Item Specifications
Florida Standards Assessments


Algebra 2 EOC Item Specifications
Florida Standards Assessments

| MAFS.912.A-SSE.2.3 <br> Also assesses <br> MAFS.912.A-SSE.1.1 <br> Also assesses <br> MAFS.912.A-SSE.1.2 | Choose and produce an equivalent form of an expression to reveal and explain properties of the quantity represented by the expression. <br> a. Factor a quadratic expression to reveal the zeros of the function it defines. <br> b. Complete the square in a quadratic expression to reveal the maximum or minimum value of the function it defines. <br> c. Use the properties of exponents to transform expressions for exponential functions. For example, the expression $1.15^{t}$ can be rewritten as $\left(1.15^{1 / 12}\right)^{12} \approx(1.012)^{12 t}$ to reveal the approximate equivalent monthly interest rate if the annual rate is $15 \%$. <br> Interpret expressions that represent a quantity in terms of its context. <br> a. Interpret parts of an expression, such as terms, factors, and coefficients. <br> b. Interpret complicated expressions by viewing one or more of their parts as a single entity. For example, interpret $P(1+r)^{n}$ as the product of $P$ and a factor not depending on $P$. <br> Use the structure of an expression to identify ways to rewrite it. For example, see $x^{4}-y^{4}$ as $\left(x^{2}\right)^{2}-\left(y^{2}\right)^{2}$, thus recognizing it as a difference of squares that can be factored as $\left(x^{2}-y^{2}\right)\left(x^{2}+y^{2}\right)$. |
| :---: | :---: |
| Item Types | Drag and drop response - May require sorting expressions. <br> Equation response - May require creating an equivalent expression or numerical response. <br> Multiple-choice response - May require selecting an expression or a value from a set of options. <br> Multi-select response - May require selecting expressions or values from a set of options. <br> Natural Language response - May require constructing a written response. |
| Clarifications | Students will use equivalent forms of a quadratic expression to interpret the expression's terms, factors, zeros, maximum, minimum, coefficients, or parts in terms of the real-world situation the expression represents. Students will use equivalent forms of an exponential expression to interpret the expression's terms, factors, coefficients, or parts in terms of the real-world situation the expression represents. <br> Students will rewrite algebraic expressions in different equivalent forms by recognizing the expression's structure. <br> Students will rewrite algebraic expressions in different equivalent forms using factoring techniques (e.g., common factors, grouping, the difference of two squares, the sum or difference of two cubes, or a combination of methods to factor completely) or simplifying expressions (i.e., combining like terms, using the distributive property, and using other operations with polynomials). |
| Assessment Limits | In items that require students to factor quadratics, the quadratic can have rational coefficients. <br> Items can have a greatest common factor that is a monomial with no more than two variables. <br> In items that require students to write equivalent expressions by |

Algebra 2 EOC Item Specifications
Florida Standards Assessments

|  | factoring, the given expression can be a difference of two squares, a <br> quadratic with rational coefficients, a sum and difference of cubes, or a <br> polynomial with the highest degree of 3. |
| :--- | :--- |
| Stimulus Attributes | Items that require interpretation should be set in a real-world context. <br> Items that require an equivalent expression found by factoring can be in <br> a real-world or mathematical context. <br> Items can use function notation. |
| Response Attribute | Items may require the student to choose and interpret units. |
| Calculator | Neutral |

Algebra 2 EOC Item Specifications
Florida Standards Assessments

| MAFS.912.N-CN.3.7 <br> Also assesses <br> MAFS.912.A-REI.2.4 | Solve quadratic equations with real coefficients that have complex solutions. <br> Solve quadratic equations in one variable. <br> a. Use the method of completing the square to transform any quadratic equation in x into an equation of the form $(\mathrm{x}-\mathrm{p})^{2}=\mathrm{q}$ that has the same solutions. Derive the quadratic formula from this form. <br> b. Solve quadratic equations by inspection (e.g., for $x^{2}=49$ ), taking square roots, completing the square, the quadratic formula, and factoring, as appropriate to the initial form of the equation. Recognize when the quadratic formula gives complex solutions and write them as $a \pm b i$ for real numbers a and b . |
| :---: | :---: |
| Item Types | Drag and drop response - May require rearranging equations. Equation response - May require creating a value or an expression. Multiple-choice response - May require selecting a value or an expression from a list. <br> Multi-select response - May require selecting multiple values. |
| Clarifications | Students will rewrite a quadratic equation in vertex form by completing the square. <br> Students will solve a quadratic equation by choosing an appropriate method (i.e., completing the square, the quadratic formula, or factoring). |
| Assessment Limits | Items may have complex solutions. <br> Items may require the student to recall from memory the quadratic formula. |
| Stimulus Attributes | Items should be set in a mathematical context. Items can use function notation. |
| Response Attribute | Items may require the student to recognize equivalent solutions to the quadratic equation. |
| Calculator | Neutral |

Algebra 2 EOC Item Specifications
Florida Standards Assessments

| MAFS.912.G-GPE.1.2 | Derive the equation of a parabola given a focus and directrix. |
| :--- | :--- |
| Item Type | Equation response - May require constructing an equation for a <br> parabola. |
| Clarification | Students will write the equation of a parabola when given the focus and <br> directrix. |
| Assessment Limit | The directrix should be parallel to a coordinate axis. |
| Stimulus Attributes | Items can be set in a mathematical or real-world context. <br> Items can use function notation. |
| Response Attribute | Items may require the student to recognize equivalent forms of an <br> equation. |
| Calculator | Neutral |

Algebra 2 EOC Item Specifications
Florida Standards Assessments

| MAFS.912.F-BF.1.2 <br> Also assesses <br> MAFS.912.F-BF.1.1 | Write arithmetic and geometric sequences both recursively and with an explicit formula, use them to model situations, and translate between the two forms. <br> Write a function that describes a relationship between two quantities. <br> a. Determine an explicit expression, a recursive process, or steps for calculation from a context. <br> b. Combine standard function types using arithmetic operations. For example, build a function that models the temperature of a cooling body by adding a constant function to a decaying exponential, and relate these functions to the model. <br> c. Compose functions. For example, if $T(y)$ is the temperature in the atmosphere as a function of height and $h(t)$ is the height of a weather balloon as a function of time, then $T(b(t))$ is the temperature at the location of the weather balloon as a function of time. |
| :---: | :---: |
| Also assesses <br> MAFS.912.A-SSE.2.4 | Derive the formula for the sum of a finite geometric series (when the common ratio is not 1), and use the formula to solve problems. For example, calculate mortage payments. |
| Item Types | Equation response - May require creating a value, an expression, or a function or showing steps for a calculation. <br> Movable text response - May require ordering steps. <br> Multiple-choice response - May require selecting a choice from a set of possible choices. <br> Natural Language response - May require explaining and interpreting a resulting function. <br> Table response - May require completing missing cells in a table. |
| Clarifications | Students will write an arithmetic sequence using a recursive formula to model a real-world context. <br> Students will write an arithmetic sequence using an explicit formula to model a real-world context. <br> Students will write a geometric sequence using a recursive formula to model a real-world context. <br> Students will write a geometric sequence using an explicit formula to model a real-world context. <br> Students will rewrite recursive formulas using an explicit formula and vice versa. <br> Students will write an explicit function, define a recursive process, or complete a table of calculations that can be used to mathematically define a real-world context. <br> Students will write a function that combines functions using arithmetic operations and relate the result to the context of the problem. Students will write a function to model a real-world context by composing functions and the information within the context. Students will use the formula for a sum of a finite geometric series to solve real-world problems. <br> Students will derive the formula for a sum of a finite geometric series where $r$ is not equal to 1 . |

Algebra 2 EOC Item Specifications
Florida Standards Assessments

| Assessment Limit | Items will not expect the student to find the sum of an infinite geometric <br> series. |
| :--- | :--- |
| Stimulus Attributes | Items should be set in a real-world context. <br> Items can use function notation. <br> In items where students have to find the sum of a finite geometric series, <br> the student will be expected to know the formula. <br> A series can be written in summation notation. |
| Response Attributes | In items where students have to give a recursive formula, the student will <br> be expected to give the initial condition and the recursion formula. <br> Items may require the student to complete algebraic steps in a deviation <br> of the formula for the sum of a geometric series. <br> Items may require the student to rearrange steps in an algebraic deviation <br> of the formula for the sum of a geometric series. <br> Items that ask the student to derive the formula for the sum of a <br> geometric series may use equivalent forms of the formula. <br> Items may require the student to choose and interpret units. |
| Calculator | Neutral |

Algebra 2 EOC Item Specifications
Florida Standards Assessments

| MAFS.912.F-BF.2.3 | Identify the effect on the graph of replacing $\mathrm{f}(\mathrm{x})$ by $\mathrm{f}(\mathrm{x})+k, k \mathrm{f}(\mathrm{x}), \mathrm{f}(\mathrm{kx})$, <br> and $\mathrm{f}(\mathrm{x}+k$ ) for specific values of k (both positive and negative); find the <br> value of $k$ given the graphs. Experiment with cases and illustrate an <br> explanation of the effects on the graph using technology. Include <br> recognizing even and odd functions from their graphs and algebraic expressions for <br> them |
| :--- | :--- |
| Item Types | Drag and drop response - May require rearranging equations. <br> Equation response - May require creating a value or an expression. <br> Graphic response - May require plotting points or a transformed <br> function. <br> Multiple-choice response - May require selecting a graph or a table from <br> a list. |
| Clarifications | Students will determine the value of $k$ when given a graph of the <br> function and its transformation. <br> Students will identify differences and similarities between a function and <br> its transformation. <br> Students will identify a graph of a function given a graph or a table of a <br> transformation and the type of transformation that is represented. <br> Students will graph by applying a given transformation to a function. <br> Students will identify ordered pairs of a transformed graph. <br> Students will complete a able for a transformed function. <br> Students will recognize even and odd functions from their graphs and <br> equations. |
| Assessment Limits | Functions can be linear, quadratic, or exponential with integral <br> exponents. <br> Functions can also be represented using tables or graphs. <br> Functions can have closed domains. <br> Functions can be discontinuous. <br> Items should have at least two transformations. |
| Response Attributes | Items should be set in a mathematical context. <br> Items can use function notation. |
| Ctimulus Attributes | Items may require the student to explain or justify a transformation that <br> has been applied to a function. <br> Items may require students to explain how a graph is affected by a value <br> of $k$. <br> Items may require students to find the value of $k$. <br> Items may require a student to complete a table of values. |
| Neutral |  |

Algebra 2 EOC Item Specifications
Florida Standards Assessments

| MAFS.912.F-BF.2.4 | Find inverse functions. <br> a. Solve an equation of the form $\mathrm{f}(\mathrm{x})=\mathrm{c}$ for a simple function, f , that has an inverse and write an expression for the inverse. For example, $f(x)=2 x^{3}$ or $f(x)=(x+1) /(x-1)$ for $x \neq 1$. <br> b. Verify by composition that one function is the inverse of another. <br> c. Read values of an inverse function from a graph or a table, given that the function has an inverse. <br> d. Produce an invertible function from a non-invertible function by restricting the domain. |
| :---: | :---: |
| Item Types | Equation response - May require expressing a function or showing steps to find the inverse of a function. <br> Graphic response - May require plotting points on a coordinate plane. Multiple-choice response - May require selecting a choice from a set of possible choices. |
| Clarifications | Students will find the inverse of a function. <br> Students will use composition of functions to determine if two functions are inverses. <br> Students will use a graph or a table of a function to determine values of the function's inverse. <br> Students will restrict the domain of a function whose inverse is not a function so that the inverse will be a function. |
| Assessment Limit | In items that require the student to find the inverse of a function, functions can consist of linear functions, quadratics of the form $f(x)=a x^{2}+c$, radical functions with a linear function as the radicand, and rational functions whose numerator is a integer and whose denominator is a linear function. |
| Stimulus Attributes | Items can be set in a real-world or mathematical context. Items can use function notation. |
| Response Attribute | Interval notation may be used to represent the domain. |
| Calculator | Neutral |

Algebra 2 EOC Item Specifications
Florida Standards Assessments

| MAFS.912.F-IF.2. 4 <br> Also assesses <br> MAFS.912.F-IF.3. 9 | For a function that models a relationship between two quantities, interpret key features of graphs and tables in terms of the quantities and sketch graphs showing key features given a verbal description of the relationship. Key features include: intercepts; intervals where the function is increasing, decreasing, positive, or negative; relative maximums and minimums; symmetries; end behavior; and periodicity. |
| :---: | :---: |
| Also assesses <br> MAFS.912.F-IF.2.5 | Compare properties of two functions each represented in a different way (algebraically, graphically, numerically in tables, or by verbal descriptions). For example, given a graph of one quadratic function and an algebraic expression for another, say which has the larger maximum. |
| Also assesses <br> MAFS.912.F-LE.2.5 | Relate the domain of a function to its graph and, where applicable, to the quantitative relationship it describes. For example, if the function $b(n)$ gives the number of person-bours it takes to assemble n engines in a factory, then the positive integers would be an appropriate domain for the function. |
|  | Interpret the parameters in a linear or an exponential function in terms of a context. |
| Item Types |  |
|  | Drag and drop response - May require rearranging comparisons and labeling key features. |
|  | Equation response - May require expressing a value, an inequality, an expression, or a function. |
|  | Multiple-choice response - May require selecting a choice from a set of possible choices. |
|  | Natural Language response - May require explaining the relationship of key features. <br> Table response - May require completing a table of values. |
| Clarifications |  |
|  | Students will determine and relate the key features of a function within a real-world context by examining the function's table. |
|  | Students will determine and relate the key features of a function within a real-world context by examining the function's graph. |
|  | Students will use a given verbal description of the relationship between two quantities to label key features of a graph of a function that models the relationship. |
|  | Students will differentiate between different types of functions using a variety of descriptors (e.g., graphical, verbal, numerical, and algebraic). Students will compare properties of two functions using a variety of function representations (e.g., algebraic, graphical, numerical in tables, or verbal descriptions). |
|  | Students will interpret the domain of a function within the real-world context given. |
|  | Students will interpret statements that use function notation within the real-world context given. |
|  | Students will determine the feasible domain of a function in relation to its graph and/or the quantitative relationship it describes. Students will interpret the rate of change and the intercepts of a linear function given in a real-world context. |

Algebra 2 EOC Item Specifications
Florida Standards Assessments

|  | Students will interpret the parameters of an exponential function given <br> in a real-world context. |
| :--- | :--- |
| Assessment Limits | Functions can be polynomial, rational, square root, absolute value, piece- <br> wise, exponential, or logarithmic. <br> In items requiring students to find the domain from graphs, <br> relationships can be on a closed or open interval. <br> In items requiring students to find the domain from graphs, <br> relationships may be discontinuous. <br> Items may have domains expressed using inequalities or interval <br> notation. <br> Key features include x-intercepts; y-intercepts; intervals where the <br> function is increasing, decreasing, positive, or negative; relative <br> maximums and minimums; symmetries; end behavior; and periodicity. |
| Stimulus Attributes | Items should be set in a real-world context. <br> Items can use function notation. |
| Response Attributes | Items may require students to write domains using inequalities or <br> interval notation. <br> Items may require the student to choose and interpret units. |
| Calculator | Neutral |

Algebra 2 EOC Item Specifications
Florida Standards Assessments

| MAFS.912.F-IF.3.8 <br> Also assesses <br> MAFS.912.A-APR.2.3 <br> Also assesses <br> MAFS.912.F-IF.2.6 <br> Also assesses <br> MAFS.912.F-IF.3.7a, b, c, d, and e. | Write a function defined by an expression in different but equivalent forms to reveal and explain different properties of the function. <br> a. Use the process of factoring and completing the square in a quadratic function to show zeros, extreme values, and symmetry of the graph, and interpret these in terms of a context. <br> b. Use the properties of exponents to interpret expressions for exponential functions. For example, identify percent rate of change in functions such as $y=(1.02)^{t}, y=(0.97)^{t}, y=(1.01)^{12 t}$, and $y=(1.2)^{1 / 10}$ and classify them as representing exponential growth or decay. <br> Identify zeros of polynomials when suitable factorizations are available and use the zeros to construct a rough graph of the function defined by the polynomial. <br> Calculate and interpret the average rate of change of a function (presented symbolically or as a table) over a specified interval. Estimate the rate of change from a graph. <br> Graph functions expressed symbolically and show key features of the graph by hand in simple cases and using technology for more complicated cases. <br> a. Graph linear and quadratic functions and show intercepts, maxima, and minima. <br> b. Graph square root, cube root, and piecewise-defined functions, including step functions and absolute value functions. <br> c. Graph polynomial functions, identifying zeros when suitable factorizations are available and showing end behavior. <br> d. Graph rational functions, identifying zeros and asymptotes when suitable factorizations are available and showing end behavior. <br> e. Graph exponential and logarithmic functions, showing intercepts and end behavior, and trigonometric functions, showing period, midline, and amplitude and using phase shift |
| :---: | :---: |
| Item Types | Drag and drop response - May require identifying key features. <br> Equation response - May require creating a value, an expression, or an equation. <br> Graphic response - May require plotting points, key features, or an equation on a graph. <br> Hot spot response - May require selecting key features on a graph. <br> Multiple-choice response - May require selecting from a list, a statement <br> about the rate of a data display, an interpretation, or context. <br> Multi-select response - May require selecting multiple responses or multiple statements about the rate of change. <br> Natural Language response - May require explaining and interpreting a function. |


| Clarifications | Students will calculate and interpret the average rate of change of a <br> continuous function that is represented algebraically, in a table of values, <br> on a graph, or as a set of data with a real-world context. <br> Students will identify zeros, extreme values, and symmetry of a quadratic <br> function written symbolically. <br> Students will classify the exponential function as exponential growth or <br> decay by examining the base, and students will give the rate of growth or <br> decay. <br> Students will use the properties of exponents to write an exponential <br> function defined by an expression in different but equivalent forms to <br> reveal and explain different properties of the function, and students will <br> determine which form of the function is the most appropriate for <br> interpretation for a real-world context. <br> Students will find the zeros of a polynomial function when the <br> polynomial is in factored form. <br> Students will identify a rough graph of a polynomial function in factored <br> form by examining the zeros of the function. <br> Students will use the x-intercepts of a polynomial function and end <br> behavior to graph the function. <br> Students will identify x- and y-intercepts and the slope of the graph of a <br> linear function. <br> Students will identify zeros, extreme values, and symmetry of the graph <br> of a quadratic function symbolically. <br> Students will identify intercepts and end behavior for an exponential <br> function. <br> Students will graph a linear function using key features. <br> Students will graph a quadratic function using key features. <br> Students will graph an exponential function using key features. <br> Students will identify and interpret key features of a graph within the <br> real-world context that the function represents. |
| :--- | :--- |
| Cesponse Attribute | In items that require the student to graph polynomial functions, the <br> polynomial's degree should be no greater than 6. |
| Calculator | Items can be set in a mathematical or real-world context. <br> Items can use function notation. <br> Items should not require the student to complete a sign chart for a <br> polynomial. |
| Items may require the student to choose and interpret units. |  |$|$| Neutral |
| :--- |

Algebra 2 EOC Item Specifications
Florida Standards Assessments

| MAFS.912.F-LE.1.4 | For exponential models, express as a logarithm the solution to $a b^{t}=d$, <br> where $a, c$, and $d$ are numbers and the base, $b$, is 2,10, or e; evaluate the <br> logarithm using technology. <br> MAFS.912.F-BF.2.a <br> Use the change of base formula. |
| :--- | :--- |
| Item Types | Equation response - May require creating a value, an expression, or an <br> equation. <br> Multi-select response - May require selecting responses from a set of <br> possible choices. |
| Clarifications | Students will use logarithms to solve exponential functions with a base <br> of 2, 10, or e. <br> Students will use the base change formula to find values of logarithms <br> with bases other than 10 and e. |
| Assessment Limit | N/A |
| Stimulus Attributes | Items should be set in a real-world context. <br> Items can use function notation. |
| Response Attribute | Items may require the student to leave the answer as a logarithm or to <br> find the value using a calculator. |
| Calculator | Neutral |

Algebra 2 EOC Item Specifications
Florida Standards Assessments

| MAFS.912.F-TF.1.2 <br> Also assesses <br> MAFS.912.F-TF.1.1 <br> Also assesses <br> MAFS.912.F-TF.3.8 | Explain how the unit circle in the coordinate plane enables the extension of trigonometric functions to all real numbers, interpreted as radian measures of angles traversed counterclockwise around the unit circle. <br> Understand radian measure of an angle as the length of the arc on the unit circle subtended by the angle; convert between degrees and radians. <br> Prove the Pythagorean identity $\sin ^{2}(\theta)+\cos ^{2}(\theta)=1$ and use it to calculate trigonometric ratios. |
| :---: | :---: |
| Item Types | Equation response - May require creating a value, an expression, or an equation. <br> Graphic response - May require drawing an angle or plotting a point on the unit circle. <br> Hot spot response - May require ordering the steps in a proof. <br> Movable text response - May require ordering the steps in a proof. <br> Natural Language response - May require explaining a relationship. <br> Selectable text response - May require highlighting a step in an informal argument. |
| Clarifications | Students will extend right triangle trigonometry to the unit circle to determine an ordered pair that lies on the unit circle. <br> Students will explain how using the radian measure of an angle traversed allows for trigonometric functions to be extended to all real numbers. Students will explain how the radian measure of an angle is the length of the arc on the unit circle subtended by the angle. <br> Students will convert the degree measure to radian measure. Students will convert the radian measure to degree measure. Students will use their knowledge of trigonometric ratios and the Pythagorean theorem to prove the Pythagorean identity. Students will use the Pythagorean identity to calculate trigonometric ratios. |
| Assessment Limits | In items where students extend right triangle trigonometry to the unit circle, the items should give an angle that is measured counterclockwise from the positive ray of the x -axis. <br> Trigonometric functions are limited to sine and cosine. <br> In items where students have to calculate trigonometric ratios, the value of either sine or cosine of an unknown angle must be given. Common sine and cosine ratios such as $\frac{1}{2}, \frac{\sqrt{2}}{2}$ and $\frac{\sqrt{3}}{2}$ should not be used in these items. |
| Stimulus Attributes | Items should be set in a mathematical or real-world context. Items can use function notation. |
| Response Attribute | Items may ask the student to complete steps in a proof of the Pythagorean identity. |
| Calculator | Neutral |

Algebra 2 EOC Item Specifications
Florida Standards Assessments

| MAFS.912.F-TF.2.5 | Choose trigonometric functions to model periodic phenomena with <br> specified amplitude, frequency, and midline. |
| :--- | :--- |
| Item Types | Equation response - May require creating a value or an equation. <br> Graphic response - May require plotting a point. <br> Multiple-choice response - May require selecting a choice from a set of <br> possible choices. <br> Multi-select response - May require selecting multiple statements about a <br> given trigonometric function. |
| Clarification | Students will interpret a real-world context to choose a trigonometric <br> function that models it. |
| Assessment Limit | Trigonometric functions are limited to sine and cosine functions that <br> model simple periodic phenomena such as harmonic motion. |
| Stimulus Attributes | Items should be set in a real-world context. <br> Items can use function notation. <br> Items may provide a graph of a trigonometric function that models a <br> real-world situation. |
| Response Attributes | Students may be asked to complete a function that models a real-world <br> context by providing missing values. <br> Items may require the student to choose and interpret units. |
| Calculator | Neutral |

Algebra 2 EOC Item Specifications
Florida Standards Assessments

| MAFS.912.N-CN.1.2 | Use the relation $i^{2}=-1$ and the commutative, associative, and <br> distributive properties to add, subtract, and multiply complex numbers. <br> Also assesses <br> MAFS.912.N-CN.1.1 |
| :--- | :--- |
| Know there is a complex number, $i$, such that $i^{2}=-1$, and every complex |  |
| number has the form a $+\mathrm{b} i$ with a and b real. |  |$|$| Equation response - May require providing a numeric value or an |
| :--- | :--- |
| expression. |
| Multi-select response - May require selecting a choice from a set of |
| possible choices. |


| MAFS.912.N-RN.1.2 | Rewrite expressions involving radicals and rational exponents using the <br> properties of exponents. <br> Also assesses |
| :--- | :--- |
| Explain how the definition of the meaning of rational exponents follows <br> from extending the properties of integer exponents to those values, <br> allowing for a notation for radicals in terms of rational exponents. For <br> example, we define $5^{\left(\frac{1}{3}\right)}$ to be the cube root of 5 because we want <br> $\left(5^{\left(\frac{1}{3}\right)}\right)^{3}=5^{\left(\frac{1}{3}\right)^{3}}$ to bold, so $\left(5^{\left(\frac{1}{3}\right)}\right)^{3}$ must equal 5. |  |
| Item Types | Drag and drop response - May require identifying parts of an algebraic <br> proof. <br> Equation response - May require creating a value or an expression. <br> Movable text response - May require ordering steps in an algebraic <br> proof. <br> Multiple-choice response - May require selecting a value or an <br> expression from a list. <br> Multi-select response - May require selecting multiple values. <br> Natural Language response - May require explaining why two rational <br> exponent expressions are equivalent or why two expressions are <br> equivalent. <br> Selectable text response - May require highlighting a step in an informal <br> argument. |
| Clarifications | Students will use the properties of exponents to rewrite a radical <br> expression as an expression with a rational exponent. <br> Students will use the properties of exponents to rewrite an expression <br> with a rational exponent to a radical expression. <br> Students will apply the properties of operations of integer exponents to <br> expressions with rational exponents. <br> Students will apply the properties of operations of integer exponents to <br> radical expressions. |
| N/A | Items should be set in a mathematical context. |
| Calculator | Items may require students to determine equivalent expressions or <br> equations. |
| Stimulus Attribute | No |

Algebra 2 EOC Item Specifications
Florida Standards Assessments

| MAFS.912.S-CP.1.1 | Describe events as subsets of a sample space (the set of outcomes) using <br> characteristics (or categories) of the outcomes, or as unions, <br> intersections, or complements of other events ("or," "and," "not"). |
| :--- | :--- |
| Item Types | Drag and drop response - May require interacting with a Venn diagram <br> by placing numeric values accordingly. <br> Equation response - May require writing a sample space. <br> Hot Spot response - May require clicking areas within a Venn diagram <br> to illustrate subsets. <br> Multiple-choice response - May require choosing a sample space. <br> Multi-select response - May require choosing lists. |
| Clarifications | Students will determine events that are subsets of a sample space. <br> Students will determine the sample space of an event by describing it as a <br> union of the subsets of other sample spaces. <br> Students will determine the sample space of an event by describing it as <br> an intersection of the subsets of other sample spaces. <br> Students will determine the sample space of an event by describing it as a <br> complement of another sample space. |
| Assessment Limits | Unions can be described verbally or use the notation A UB . <br> Intersections can be described verbally or use the notation A $\cap B$ <br> Complements can be described verbally or use the notation $\sim$ A. |
| Items should not ask the student to determine probability. |  |
| Items should not require the student to apply understanding of |  |
| independence or dependence. |  |$|$

Algebra 2 EOC Item Specifications
Florida Standards Assessments


Algebra 2 EOC Item Specifications
Florida Standards Assessments

|  | together. <br> Students will use given probabilities to determine if two events are <br> independent. <br> Students will find the conditional probability of A given B and the <br> conditional probability of B given A to determine if A and B are <br> independent events. <br> Students will find the conditional probability of A given B as the fraction <br> of B's outcomes that belong to A. <br> Students will interpret a conditional probability in terms of a real-world <br> context. |
| :--- | :--- |
| Assessment Limits | Items may use Venn diagrams. <br> Unions can be described verbally or use the notation A $\cup \mathrm{B}$. <br> Intersections can be described verbally or use the notation A $\cap \mathrm{B} \mathrm{}$. <br> Complements can be described verbally or use the notation $\sim$ A. |
| Stimulus Attribute | Items should be set in a real-world context. |

Algebra 2 EOC Item Specifications
Florida Standards Assessments

| MAFS.912.S-CP.2.7 | Apply the Addition Rule, $\mathrm{P}(\mathrm{A}$ or B$)=\mathrm{P}(\mathrm{A})+\mathrm{P}(\mathrm{B})-\mathrm{P}(\mathrm{A}$ and B), and <br> interpret the answer in terms of the model. |
| :--- | :--- |
| Item Types | Equation response - May require identifying a value. <br> Multiple-choice response - May require selecting a numeric value. <br> Natural Language response - May require interpreting the Addition Rule <br> within a context. |
| Clarification | Students will find probabilities using the Addition Rule and interpret the <br> answer within the real-world context. |
| Assessment Limit | Data can be displayed in a two-way table, a Venn diagram, a tree <br> diagram, or simply described. |
| Stimulus Attribute | Items should be set in a real-world context. |
| Response Attribute | Students may be asked to find the unknown value when given three of <br> the values in $\mathrm{P}(\mathrm{A}$ or B$)=\mathrm{P}(\mathrm{A})+\mathrm{P}(\mathrm{B})-\mathrm{P}(\mathrm{A}$ and B$)$. |
| Calculator | Neutral |

Algebra 2 EOC Item Specifications
Florida Standards Assessments

| MAFS.912.S-IC.1.1 | Understand statistics as a process for making inferences about <br> population parameters based on a random sample from that <br> population. |
| :--- | :--- |
| Item Types | Equation response - May require the student identifying a quantity. <br> Multiple-choice response - May require selecting a choice from a set of <br> possible choices. <br> Natural Language response - May require describing flaws in data <br> collection or interpretation or recommending a correct course of action. |
| Clarifications | Students will use observed results from a random sample to make an <br> inference about the population. |
| Assessment Limits | Items may require students to distinguish between a statistic and a <br> parameter. <br> Items may require a student to be familiar with different kinds of <br> sampling methods but not the specific names of the methods. |
| Items may require a student to be familiar with the process of statistical <br> inference but not require the student to state the process. |  |
| Stimulus Attribute | Items should be set in a real-world context. |
| Response Attribute | Items may require the student to choose and interpret units. |
| Calculator | No |

Algebra 2 EOC Item Specifications
Florida Standards Assessments
$\left.\begin{array}{|l|l|}\hline \text { MAFS.912.S-IC.2.3 } & \begin{array}{l}\text { Recognize the purposes of and differences among sample surveys, } \\ \text { Also assesses } \\ \text { MAFSeriments, and observational studies; explain how randomization } \\ \text { relates to each. }\end{array} \\ \text { Also assesses } \\ \text { Decide if a specified model is consistent with results from a given data- } \\ \text { MAFS.912.S-IC.2.4 } \\ \text { generating process (e.g., using simulation). For example, a model says a } \\ \text { spinning coin falls seads up with probability 0.5. Would a result of 5 tails in a row } \\ \text { cause you to question the model? } \\ \text { Also assesses } \\ \text { MAFS.912.S-IC.2.5 }\end{array} \quad \begin{array}{l}\text { Use data from a sample survey to estimate a population mean or } \\ \text { proportion; develop a margin of error through the use of simulation } \\ \text { models for random sampling. } \\ \text { Also assesses } \\ \text { MAFS.912.S-IC.2.6 }\end{array} \begin{array}{l}\text { Use data from a randomized experiment to compare two treatments; use } \\ \text { simulations to decide if differences between parameters are significant. } \\ \text { Evaluate reports based on data. }\end{array}\right\}$

Algebra 2 EOC Item Specifications
Florida Standards Assessments

| MAFS.912.S-ID.1.4 | Use the mean and standard deviation of a data set to fit it to a normal <br> distribution and to estimate population percentages. Recognize that <br> there are data sets for which such a procedure is not appropriate. Use <br> calculators, spreadsheets, and tables to estimate areas under the normal <br> curve. |
| :--- | :--- |
| Item Types | Multiple-choice response - May require selecting a correct comparison. <br> Multi-select response - May require choosing statements about a <br> comparison. <br> Natural Language response - May require explaining a comparison. |
| Clarifications | Student will calculate the $z$-score and use it to compare a data point to <br> the population. <br> Student will calculate the z-score and use it to compare two data points. |
| Assessment Limit | Items should contain data that are approximately normally distributed. |
| Stimulus Attributes | Items should be set in a real-world context. <br> Items should include a partial or full standard normal distribution table. <br> Items should give the mean and standard deviation of the data set. |
| Response Attribute | Items should be set in a real-world context. |
| Calculator | Neutral |

