

Sec. 8.4 Rational Expressions

Write in simplest form: FACTOR & CANCEL

a.  $\frac{9x^2 + 6x}{36x + 24} = \frac{3x \cancel{(3x+2)}}{12 \cancel{(3x+2)} \neq 0} = \frac{x}{4}, x \neq -\frac{2}{3}$

b.  $\frac{1 \cdot x^2 - 3x + 2}{x+2} \cdot \frac{x^2 - 36}{x^2 + 5x - 6}$

$\frac{\cancel{(x-1)}(x-2)\cancel{(x+6)}(x-6)}{(x+2)\cancel{(x-1)}\cancel{(x+6)} \neq 0} = \frac{(x-2)(x-6)}{(x+2)}, x \neq -2, 1, -6$

$x^2 - 1x - 2x + 2 = x(x-1) - 2(x-1) = (x-1)(x-2)$

$x+2 \neq 0 \Rightarrow x \neq -2$   
 $x-1 \neq 0 \Rightarrow x \neq 1$   
 $x+6 \neq 0 \Rightarrow x \neq -6$

c.  $\frac{6x - 3x^2}{36 - x^2} \div \frac{x^3 - x^2 - 2x}{x^2 - 5x - 6}$

$\frac{6x - 3x^2}{36 - x^2} \cdot \frac{x^2 - 5x - 6}{x^3 - x^2 - 2x}$

$\frac{x^2 + 1x - 6x - 6}{x(x+1) - 6(x+1)} = \frac{(x+1)(x-6)}{(x+1)(x-6)}$

$\frac{3x \cancel{(2-x)} \cancel{(x+1)}(x-6)}{(6-x)(6+x)} \cdot \frac{x \cancel{(x+1)}(x-2)}{x \cancel{(x+1)}(x-2)}$

$0 \neq \frac{3}{(6-x)(6+x)}$

$x(x^2 - x - 2) = x(x^2 + 1x - 2x - 2) = x(x(x+1) - 2(x+1)) = x(x+1)(x-2)$

$= \frac{3}{x+6}, x \neq -6, -1, 0, 2, 6$

$\frac{x-6}{6-x} = \frac{x-6}{-(x-6)} = \frac{\cancel{(x-6)}}{-\cancel{(x-6)}} = -1$

$6-x=0 \Rightarrow x \neq 6 \checkmark$   
 $6+x=0 \Rightarrow x \neq -6 \checkmark$   
 $x=0 \Rightarrow x \neq 0 \checkmark$   
 $x+1=0 \Rightarrow x \neq -1 \checkmark$

d.  $\frac{3a^3b^3}{a-b}$

$$\div \leftarrow \frac{\frac{3a^3b^3}{a-b}}{\frac{4ab}{b-a}} = \frac{3a^3b^3}{a-b} \div \frac{4ab}{b-a}$$

$$= \frac{3a^3b^3}{(a-b)} \cdot \frac{(b-a)}{4ab}$$

*Handwritten notes:*  $a^2a$ ,  $b^2b$ ,  $\frac{2}{2}$ ,  $\frac{-1}{-1}$

$$= \frac{-3a^2b^2}{4}, a \neq 0, b \neq 0$$

*Handwritten notes:*  $a-b=0$ ,  $\frac{4}{4} \neq 0$ ,  $a=0$ ,  $b=0$ ,  $\frac{a-b=0}{+b \quad +b}$ ,  $a \neq b$ ,  $\frac{b-a=0}{+a \quad +a}$ ,  $b \neq a$

- e. Which jewelry box uses  $1c$  .naï for the bottom and for the lid if the perimeters of the boxes are the same:
- a jewelry box shaped like a circle or
  - a jewelry box shaped like a regular hexagon?
- Circle.                      Reg. Hexagon (6)