

Section 9.3 Geometric Sequences

geometric sequence: starting value a
and common ratio r

$a_1, a_1 r, a_1 r^2, a_1 r^3, \dots$
 $3, 6, 12, 24, \dots$
 $a_1 \times 2 \times 2 \times 2 \dots$
 $r = 2$

recursive definition:

$$a_n = r \cdot a_{n-1}$$

explicit definition:

$$a_n = a_1 r^{n-1}$$

Problem 1:

Is the sequence geometric? If it is, what are a_1 and r ?

a. $5, 10, 50, \dots$

$$a_1 = 5 \quad \text{no}$$

$$\frac{50}{10} \neq \frac{10}{5}$$

b. $-10, 6, -3.6, \dots$

$$a_1 = -10$$

$$r = -\frac{3}{5}$$

$$\frac{-3.6}{6} = \frac{6}{-10} = -\frac{3}{5}$$

$$\frac{3.6}{60} = \frac{6}{10} = \frac{3}{5}$$

Problem 2:

What are the second and third terms of the geometric sequence 2, 8, 32, 128?

$$\begin{aligned} \downarrow & \quad \downarrow & \boxed{a_1} & \quad \quad \quad \boxed{a_4} \rightarrow n=4 \\ a_n = a_1 r^{n-1} & & & & a_n \\ \frac{128}{2} = \frac{2r^{4-1}}{2} & \quad 64 = r^3 & & & \\ & \quad 4 = r & & & \end{aligned}$$

Problem 3:

You work as a store manager and need to clear some inventory. You decide to discount each item by 30% of the previous week's price until the entire inventory is sold. The original price of one item is \$60. What will be the cost of the item during the fifth week of the sale?

$$\begin{aligned} a_1 &= 60 & r &= (1 - 0.3) = 0.7 \\ a_n &= 60(0.7)^{n-1} & & & a_6 & y = a_6 \\ a_6 &= 60(0.7)^5 = \$10.08 & & & & a_1 r^{n-1} \end{aligned}$$

Problem 4:

What are the possible values of the missing term of the geometric sequence $\boxed{28}, a_2, \boxed{7}$?

$$\begin{aligned} r &= \frac{7}{28} = \frac{a_2}{28} \\ a_2^2 &= \sqrt{28 \cdot 7} & \text{geometric mean} \\ & \quad 4 \cdot 7 \cdot 7 \\ a_2 &= 2.7 \\ a_2 &= 14 & 28, \underline{14}, 7 \end{aligned}$$