

Sec. 7.1 Zero and Negative Exponents

$$a^0 = 1$$

$$a^{-n} = \frac{1}{a^n}$$

$$\begin{array}{ccccccc}
 3^{-2} & 3^{-1} & 3^0 & 3^1 & 3^2 & 3^3 & 3^4 \\
 \frac{1}{9} & \frac{1}{3} & 1 & 3 & 9 & 27 & 81 \\
 & \swarrow & \swarrow & \swarrow & \swarrow & \swarrow & \\
 & \div 3 & \div 3 & \div 3 & \div 3 & \div 3 &
 \end{array}$$

$$\frac{1}{3} \div 3$$

$$\frac{1}{3} \cdot \frac{1}{3} = \frac{1}{9}$$

Problem 1: Simplify

$$a. 6^{-2} = \frac{1}{6^2} = \frac{1}{36}$$

$$b. (-9.3)^0 = 1$$

Problem 2: Simplify

$$a. 3a^{-2}b^3 = 3 \cdot \frac{1}{a^2} \cdot b^3 = \frac{3b^3}{a^2}$$

$$b. \frac{1}{x^{-6}} = x^6 \qquad \frac{1}{\frac{1}{x^6}} = 1 \cdot \frac{x^6}{1} = x^6$$

$$c. \frac{4^1}{a^{-3}} = 4a^3$$

$$d. \frac{n^{-5}}{m^2} = \frac{1}{m^2 n^5}$$

Problem 3:

What is the value of $2a^{-2}b^4$ for $a = -2$ and $b = 1$?

$$2a^{-2}b^4$$

$$\frac{2b^4}{a^2} = \frac{2(1)^4}{(-2)^2} = \frac{2 \cdot 1}{4}$$

$$\boxed{\frac{1}{2}}$$

$$2(-2)^{-2}(1)^4$$

$$\frac{2(1)^4}{(-2)^2} = \frac{2 \cdot 1}{4}$$

$$\boxed{\frac{1}{2}}$$

b. $n = -2, w = 5$

$$n^{-4}w^0 = \frac{w^0}{n^4} = \frac{1}{n^4} = \frac{1}{(-2)^4} = \frac{1}{16}$$

$$* \quad -\boxed{3^0} = -1 \cdot 3^0 = -1 \cdot 1 = -1$$
$$\boxed{(-3)^0} = 1$$

Problem 4: The expression $6400 \cdot 2^t$ models a population of 6400 birds after t periods of 8 years. (The population of the birds doubles every 8 years.)

Evaluate the expression for $t = 0$ and $t = -2$.

$$6400 \cdot 2^t$$

$$6400 \cdot 2^0 = 6400 \cdot 1 = 6400$$

$$6400 \cdot 2^{-2} = 6400 \cdot \frac{1}{2^2}$$

$$= 6400 \cdot \frac{1}{4} = \boxed{1600}$$