

## Sec. 5.3 Slope - Intercept Form

## Slope - Intercept Form

$$y = mx + b$$

$\downarrow$                        $\downarrow$   
 slope                      y-intercept

Problem 1:

What are the slope and y-intercept of the graph of

$$y = 3x - 6$$

slope : 3  
 y-intercept : -6

Problem 2:

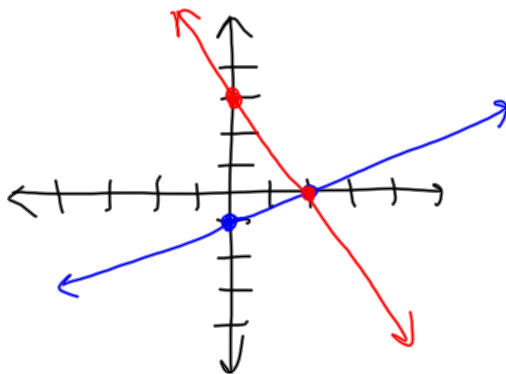
What is an equation of the line with slope 5 and y-intercept 8?

$$y = mx + b$$

$$y = 5x + 8$$

Problem 3:

What is the equation of the line?



$$y = mx + b$$

$$y = \frac{1}{2}x - 1$$

$$y = -\frac{3}{2}x + 3$$

Problem 4:

What is an equation in slope-intercept form of the line that passes through the points that follow?

a.  $(1, -6)$  and  $(-3, 10)$

$$y = mx + b \rightarrow \underline{y = -4x + b}$$

① Find slope  $m = \frac{y_2 - y_1}{x_2 - x_1} = \frac{10 - (-6)}{-3 - 1} = \frac{10 + 6}{-4} = \frac{16}{-4}$

$$m = -4$$

②

Find b.

- Pick ONE point
- Plug it in for x and y
- Plug in m.
- Solve for b.

$$\begin{matrix} x & y \\ (1, & -6) \end{matrix}$$

$$\underline{y = -4x + b}$$

$$-6 = -4(1) + b$$

$$-6 = -4 + b$$

$$\begin{array}{r} +4 & +4 \\ \hline -2 = b \end{array}$$

$$-2 = b$$

③

Write the equation, plugging in m + b.

$$m = -4 \quad b = -2$$

$$\boxed{y = -4x - 2}$$

b.  $(3, -2)$  and  $(1, -3)$

$$m = \frac{y_2 - y_1}{x_2 - x_1} = \frac{-3 - (-2)}{1 - 3} = \frac{-3 + 2}{-2} = \frac{-1}{-2}$$

$$m = \frac{1}{2} \rightarrow y = \frac{1}{2}x + b$$

$$\begin{matrix} x & y \\ (3, -2) \end{matrix} \quad -2 = \frac{1}{2}(3) + b$$

$$-2 = 1\frac{1}{2} + b$$

$$-1\frac{1}{2} \quad -1\frac{1}{2}$$


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$$-\frac{7}{2} \text{ or } -3\frac{1}{2} = b$$

$$b = -3\frac{1}{2}, \quad m = \frac{1}{2}$$

$$y = \frac{1}{2}x - 3\frac{1}{2}$$

c.  $(2, 1)$  and  $(5, -8)$

$$m = \frac{-8 - 1}{5 - 2} = \frac{-9}{3} = -3$$

$$y = -3x + b$$

$$\rightarrow y = -3x + 7$$

$(x, y)$   
 $(2, 1)$

$$1 = -3(2) + b$$

$$1 = -6 + b$$

$$\begin{array}{r} +b \quad +b \\ \hline 7 = b \end{array}$$

d.  $(-2, 4)$  and  $(3, -1)$

$$m = \frac{-1 - 4}{3 - (-2)} = \frac{-5}{5} = -1$$

$$y = -x + b$$

$(-2, 4)$

$$4 = -(-2) + b$$

$$4 = 2 + b$$

$$\begin{array}{r} -2 \quad -2 \\ \hline 2 = b \end{array}$$

$$y = -x + 2$$

Problem 5:

Graph  $y = \frac{1}{2}x - 1$

