

Direct Variation

What is it? *a linear equation whose graph goes through (0,0)*
 a relationship that can be represented by a function in the form $y = kx$, where $k \neq 0$

Constant:

$$\boxed{k = \frac{y}{x}}$$

is constant for all ordered pairs

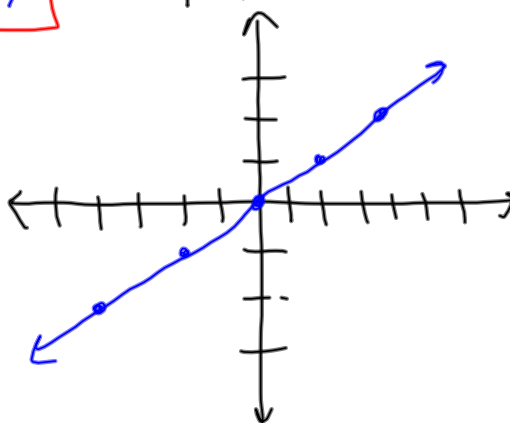
Equation:

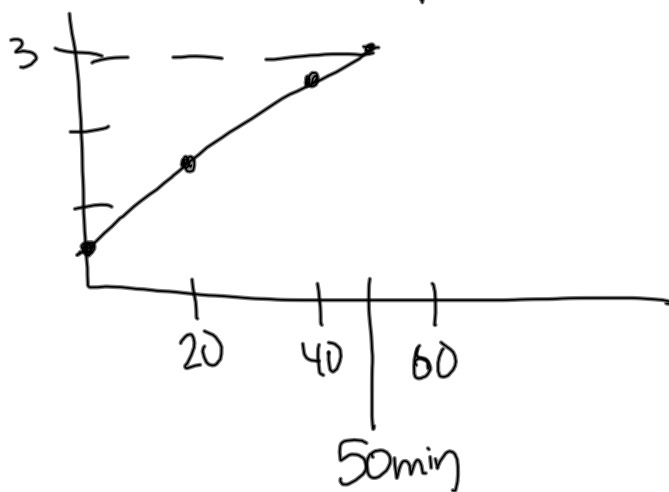
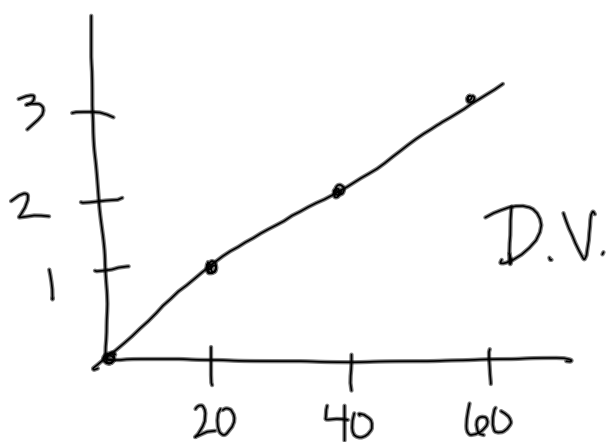
$$y = mx$$

y-int is 0
 \downarrow
 constant
 $(y = kx$
 or
 $y = ax)$

Table: $\boxed{y = \frac{1}{2}x}$ Graph.

x	y
-4	-2
-2	-1
* 0	0
2	1
4	2





Direct Variation	Not a Direct Variation																								
<div style="border: 1px solid blue; border-radius: 50%; padding: 5px; display: inline-block; margin-bottom: 10px;"> $y = mx$ </div> $5x - 2y = 0$ $y = -\frac{5}{2}x$ $-3x + 2y = 0$ $3x = 2y$ <table style="border-collapse: collapse; margin-bottom: 10px;"> <tr><td style="border-right: 1px solid black; padding: 0 5px;">x</td><td style="padding: 0 5px;">y</td></tr> <tr><td style="border-right: 1px solid black; padding: 0 5px;">3</td><td style="padding: 0 5px;">2</td></tr> <tr><td style="border-right: 1px solid black; padding: 0 5px;">3</td><td style="padding: 0 5px;">2</td></tr> <tr><td style="border-right: 1px solid black; padding: 0 5px;">9</td><td style="padding: 0 5px;">6</td></tr> </table> <table style="border-collapse: collapse;"> <tr><td style="border-right: 1px solid black; padding: 0 5px;">x</td><td style="padding: 0 5px;">y</td></tr> <tr><td style="border-right: 1px solid black; padding: 0 5px;">4</td><td style="padding: 0 5px;">8</td></tr> <tr><td style="border-right: 1px solid black; padding: 0 5px;">7</td><td style="padding: 0 5px;">14</td></tr> <tr><td style="border-right: 1px solid black; padding: 0 5px;">10</td><td style="padding: 0 5px;">20</td></tr> </table>	x	y	3	2	3	2	9	6	x	y	4	8	7	14	10	20	<div style="border: 1px solid blue; border-radius: 50%; padding: 5px; display: inline-block; margin-bottom: 10px;"> $y = mx + b$ </div> $y = \frac{3}{4}x - 7$ $x - 3y = 7$ $8x + 4y = 12$ <table style="border-collapse: collapse; margin-left: auto; margin-right: auto;"> <tr><td style="border-right: 1px solid black; padding: 0 5px;">x</td><td style="padding: 0 5px;">y</td></tr> <tr><td style="border-right: 1px solid black; padding: 0 5px;">2</td><td style="padding: 0 5px;">4</td></tr> <tr><td style="border-right: 1px solid black; padding: 0 5px;">3</td><td style="padding: 0 5px;">8</td></tr> <tr><td style="border-right: 1px solid black; padding: 0 5px;">4</td><td style="padding: 0 5px;">16</td></tr> </table>	x	y	2	4	3	8	4	16
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Problems 5.2

① $\frac{2y}{2} = \frac{3x+1}{2} \frac{1}{2}$ Is this D.V.?

$y = \frac{3}{2}x + \frac{1}{2}$ NO, $b = \frac{1}{2}$, not 0

② y varies directly with x
Write a direct variation equation.
Find the value of y when $x = 10$.

$y = 9$ when $x = 5$ $m = \frac{y}{x} = \frac{9}{5}$

$y = mx$

$\frac{9}{5} = \frac{m \cdot 5}{5}$

$\frac{9}{5} = m$

$y = \frac{9}{5}x$

$x = 10, y = \frac{9}{5} \cdot \frac{10^2}{1} = 18$

18

Notes

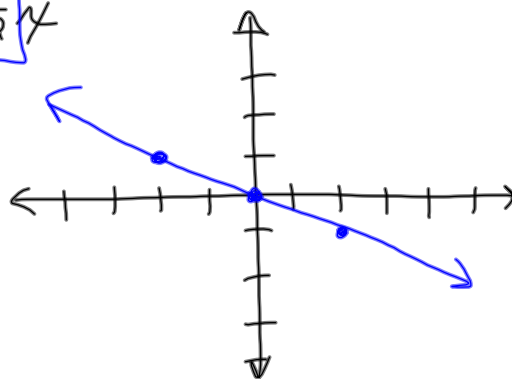
Problem 3:

Graph

$$y = \boxed{-\frac{1}{2}x}$$

x	y
-2	+1

$-\frac{1}{2}(-2)$



Problem 4:

Suppose \$15 (US) is worth about \$150 Mexican Pesos.

a. What is an equation that relates US dollars x to Mexican pesos y ?

$$y = mx$$

$$\frac{150}{15} = \frac{m \cdot 15}{15}$$

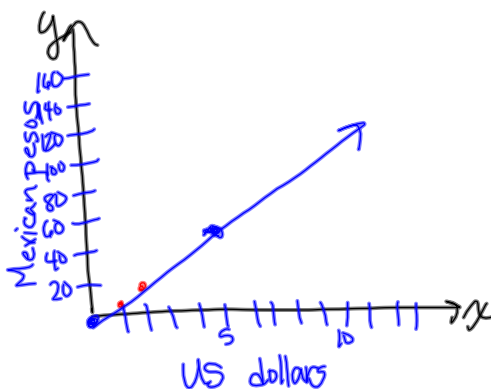
$$10 = m$$

$$m = \frac{y}{x} = \frac{150}{15}$$

$$m = 10$$

$$\boxed{y = 10x} \quad m = \frac{10}{1}$$

b. What is the graph of this equation?



x	y = 10x
5	50

Problem 5

Do these quantities vary directly?

- a. the number of ounces of cereal and the number of Calories the cereal contains

Yes, as the number of ounces **increases**, the number of Calories **increases**. When one is 0, the other is 0.

- b. the amount of money you have left and the number of items you purchase

As the number of items you purchase **increases**, the amount of money you have **decreases**

No (inverse variation)