

**Graphs, Parents**

$y = x$   $y = |x|$   $y = x^2$   $y = \sqrt{x}$

$y = b^x, b > 1$   $y = b^x, 0 < b < 1$

$y = \log_b x, b > 1$   $y = \log_b x, 0 < b < 1$

$(\frac{1}{5})^3 = 125$   $\log_{\frac{1}{5}} 125 = -3$   
 $(5)^3 \rightarrow 125$

$y = \frac{1}{x}$

$y = \sin x$   $y = \cos x$

$y = x^3$   $y = \sqrt[3]{x}$

$y = 3\sqrt[3]{x+2} - 1$

x	y
0	0
-1	-1
1	1
8	2

## Transformations

$$y = f(x + a) \rightarrow \text{left } a \text{ units}$$

opp.  $a > 0$

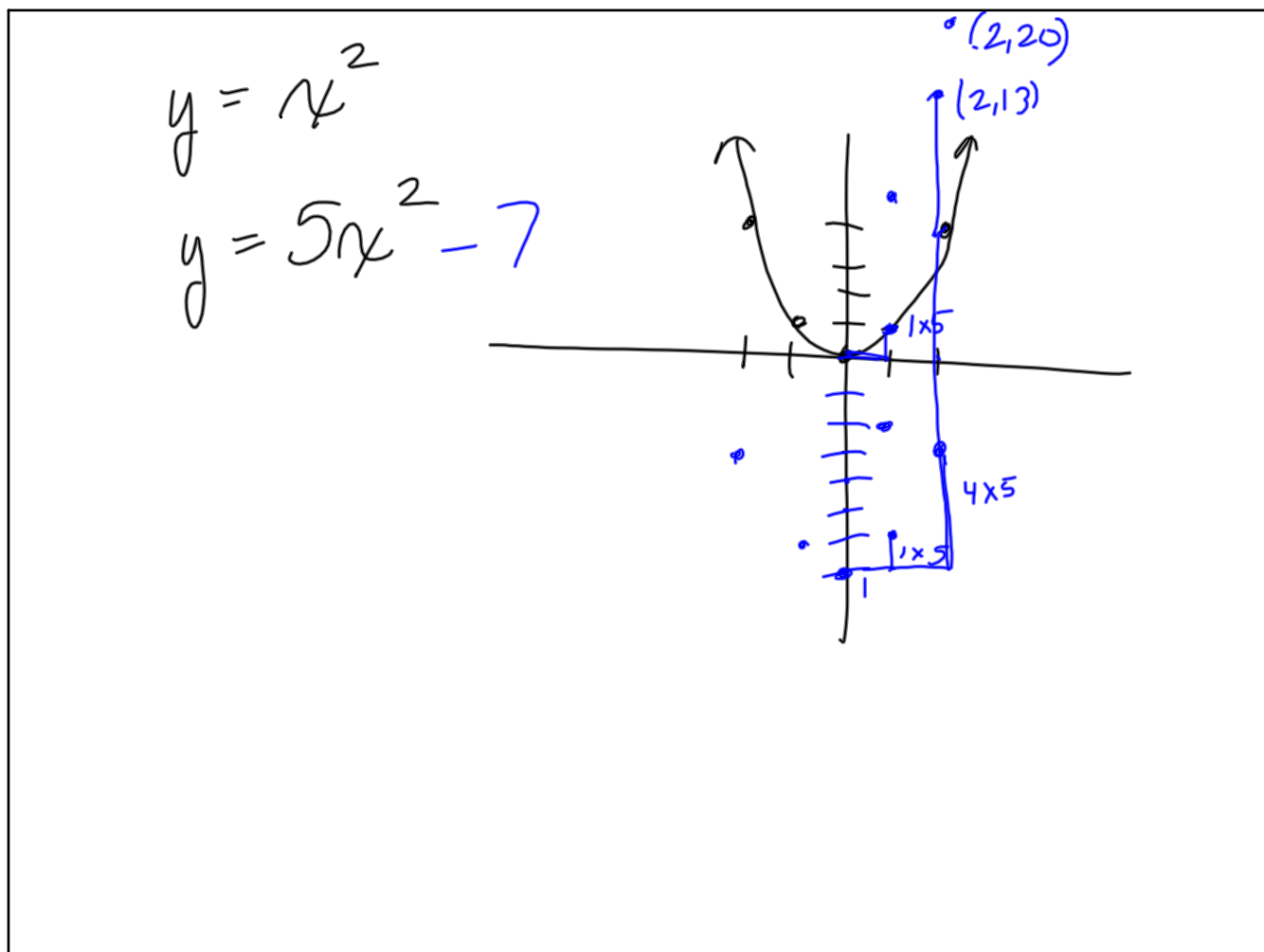
$$y = f(x - a) \rightarrow \text{right } a \text{ units}$$

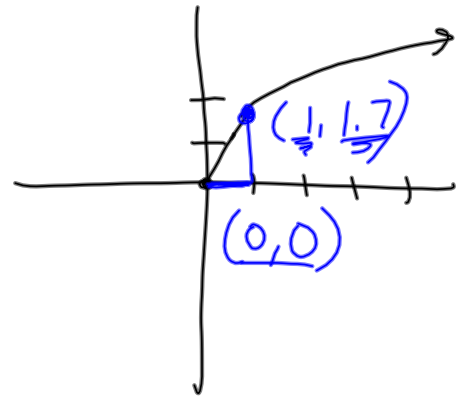
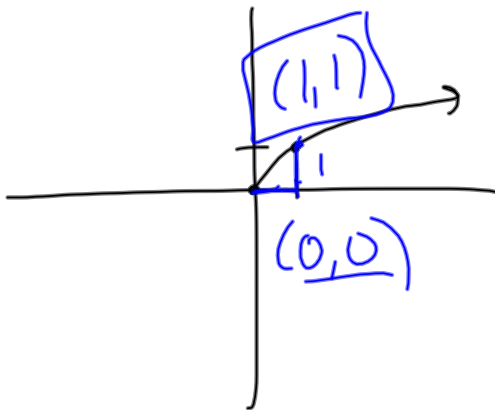
$$y = f(x) \begin{matrix} +k \\ -k \end{matrix} \begin{matrix} \leftarrow k > 0 & \text{up } k \text{ units} & f(x) + k \\ k < 0 & \text{down } k \text{ units} & f(x) - k \end{matrix}$$

$$y = -f(x) \rightarrow \text{reflection over } x\text{-axis (flip)}$$

$$y = a f(x) \begin{matrix} \nearrow a > 1 & \text{vertically stretched by a factor } a \\ \searrow 0 < a < 1 & \text{vertically compressed by a factor } a \end{matrix}$$

$$y = f(ax) \begin{matrix} \nearrow a > 1 & \text{horizontally compressed by} \\ & \text{a factor } \frac{1}{a} \\ \searrow 0 < a < 1 & \text{horizontally stretched by a} \\ & \text{factor } \frac{1}{a} \end{matrix}$$





a.  $y = 2\sqrt{x}$  —  $3 \cdot \sqrt{1} = 3$

b.  $y = \frac{1}{3}\sqrt{x}$  —  $\frac{1}{3} \cdot \sqrt{1} = \frac{1}{3}$

c.  $y = \sqrt{3x}$  —  $\sqrt{3 \cdot 1} = \sqrt{3} = 1.7$

d.  $y = \sqrt{\frac{1}{3}x}$  —  $\sqrt{\frac{1}{3} \cdot 1} = \sqrt{\frac{1}{3}} < \frac{1}{3}$