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quadratic form

$$\boxed{(4x^2+9)(2x+3)(2x-3)}$$

$$(4x^2+9)(4x^2-9)$$

Warm-up:

①  $5x^3 - 20x$

③  $|6x^4 - 8|$

$5x(x^2-4) \quad 5x(x+2)(x-2)$

②  $36x^2 - 84x + 49$

④  $|x^4 - 18x^2 + 81|$

$$\begin{array}{l} (6x-7)^2 \\ -42x \end{array}$$

$$\begin{array}{l} (x^2-9)^2 \\ [(x+3)(x-3)]^2 \end{array}$$

$(x+3)^2(x-3)^2$

$$* a^2 - b^2 = (a+b)(a-b)$$

$$* a^2 + 2ab + b^2 = (a+b)^2$$

"unfolding"

Ex:  $x^2 + \underline{7x} + \underline{12}$

$(x+3)(x+4)$

$\begin{array}{r} 3x \\ + 4x \\ \hline 7x \end{array}$

$(x+a)(x+b)$

$x^2 + \underline{bx} + \underline{ax} + ab$

$x^2 + (b+a)x + ab$

Factors of

$\frac{12}{1 \cdot 12}$   
 $2 \cdot 6$   
 $3 \cdot 4 \quad 3+4=7$

Ex:  $x^2 - 7x + 10$

$(x-2)(x-5)$

$\frac{10}{1 \cdot 10}$   
 $2 \cdot 5 \quad -2-5=-7$

Ex:  $x^2 - 6x - 16$

$(x+2)(x-8)$

$\frac{-16}{1 \cdot 16}$   
 $2 \cdot 8 \quad 2-8$   
 $4 \cdot 4$

Ex :  $a^4 - 9a^2 + 8$ .

$\frac{8}{1 \cdot 8}$   $(a^2 - 1)(a^2 - 8)$   
 $2 \cdot 4$   $(a+1)(a-1)(a^2 - 8)$   
 $-1 - 8 = -9$

Ex :  $a^2 - 7a - 30$

"quadratic form"

$\begin{matrix} a^4 & a^2 \\ (a^2) & (a^2) \end{matrix}$   
 ~~$a^3$~~   
 $\begin{matrix} a^6 & \\ (a^3) & (a^3) \end{matrix}$   
 $\begin{matrix} a^8 & \\ (a^4) & (a^4) \end{matrix}$

Homework

9.6 (2-38) eoe

9.7 (1-35) eoo