

10-3 Completing the Square

Find the value of c that makes the expression a perfect square trinomial.

Then write the expression as the square of a binomial

Ex: $x^2 + 10x + c = (x+5)^2$

Annotations: $c=25$, $5x$ $5x$, $\frac{1}{2}(10)$, 5^2 square

Ex: $x^2 + 14x + c = (x+7)^2$

Annotations: $c=49$, $\frac{1}{2}(14)$, $(\frac{b}{2})^2$, 7^2

General formula: $x^2 + bx + (\frac{b}{2})^2 = (x + \frac{b}{2})^2$

Annotations: $(a=1)$, $\frac{1}{2} \cdot b$

Ex: $x^2 - 24x + 144 = (x-12)^2$

Ex: $x^2 - 9x + c = (x - \frac{9}{2})^2$

Annotations: $c = (-\frac{9}{2})^2 = \frac{81}{4}$

Ex: $x^2 + 16x + 64 = (x+8)^2$

$\begin{matrix} \rightarrow & \boxed{\begin{matrix} 1 \cdot 6 \\ 2 \cdot 3 \end{matrix}} & \leftarrow \end{matrix}$
 $6f^2 - \frac{3}{2}f + \frac{1}{12}$
 $\begin{matrix} \rightarrow & \frac{1}{1} \cdot \frac{1}{12} \\ & \frac{1}{2} \cdot \frac{1}{6} \\ & \boxed{\frac{1}{3} \cdot \frac{1}{4}} \end{matrix}$

$(f - \frac{1}{3})(6f - \frac{1}{4})$

$(2f - \frac{1}{3})(3f - \frac{1}{4})$

$\frac{2}{4} = \frac{1}{2}$

$\frac{1}{12} \quad 12(6f^2 - \frac{3}{2}f - \frac{1}{12})$

$\frac{1}{12} (\quad)$

$\frac{1}{12} \cdot 12 (6f^2 - \frac{3}{2}f + \frac{1}{12})$

$\frac{1}{12} (72f^2 - 18f + 1)$

$\frac{1}{12} (6f - 1)(12f - 1)$

$\{ (2f - \frac{1}{3})(3f - \frac{1}{4}) \}$

$\frac{1}{4} \cdot \frac{1}{3} (6f - 1)(12f - 1)$

$\begin{matrix} 1 \cdot 72 \\ 2 \cdot 36 \\ 3 \cdot 24 \\ 4 \cdot 18 \\ 6 \cdot 12 \end{matrix}$

15. $\boxed{45x^2 - 103x^2 + 12}$
 $- 58x^2 + 12$
 $- 2(29x^2 - 6)$

Grouping : 4 terms or more

Ex: $x^3 + 7x^2 - 9x - 63$

if \ominus , take out \ominus as part of GCF
Find GCF of each group

$$\underbrace{x^3 + 7x^2}_{x^2(x+7)} - \underbrace{9x - 63}_{9(x-7)}$$

$$x^2(x+7) - 9(x-7)$$

$$(x+7)(x^2-9) \quad ax^2-9a$$

$$(x+7)(x+3)(x-3) \quad a(x^2-9)$$

Ex: $3x^2 - 5x + 9x - 15$

$$x(3x-5) + 3(3x-5)$$

$$(3x-5)(x+3)$$

Ex: $x^3 - 3x^2 - 16x + 48$

$$x^2(x-3) - 16(x-3)$$

$$(x-3)(x^2-16)$$

$$(x-3)(x-4)(x+4)$$

Sum (Difference) of Two Cubes

$$a^3 + b^3 = (a + b)(a^2 - ab + b^2)$$

$$\begin{array}{r} a^3 - \cancel{a^2b} + \cancel{ab^2} \\ a^2b - \cancel{ab^2} + b^3 \\ \hline a^3 + b^3 \end{array}$$

Ex: $w^3 + 27 = (w + 3)(w^2 - 3w + 9)$

$3w$ ↗ opposite

Ex: $27x^3 - 125$ $a^3 + b^3 = (a+b)(a^2 - ab + b^2)$

$$(3x - 5)(9x^2 + 15x + 25)$$

$-15x$ ↗ opp

Ex: $-2d^5 + 250d^2$

$$-2d^2(d^3 - 125)$$

$$-2d^2(d - 5)(d^2 + 5d + 25)$$

$-5d$

p. 54(13-21)all p. 115(11-31)odd

