

$$15. \quad 9x^2 - 12x + c$$

14. $x^2 - 9x + c$
 $(x - \frac{9}{2})^2$
 $c = \frac{81}{4}$

$$(3x - 2)^2 \quad c = 4$$

$-6x$

$$17. (x+1)^2(x^2-x+1)(x-4)$$

$$18. (3x-1)(2x^3-5)(x-6)$$

$x+1$
 $\underline{-1}$

<u>5</u>	<u>4</u>	<u>3</u>	<u>2</u>	<u>1</u>	<u>0</u>
1	-3	-4	1	-3	-4
	-1	4	0	-1	4

$$1 \quad -4 \quad 0 \quad 1 \quad -4 \quad | \quad 0$$

$$x^4 - 4x^3 + x - 4$$

$$x^3(x-4) + 1(x-4)$$

$$(x^3 + 1)(x - 4)$$

$$(x+1)^2(x^2-x+1)(x-4)$$

x^5

5. $2w^3 + 54$
 $2(w^3 + 27)$
 $2(w+3)(w^2 - 3w + 9)$

$\begin{matrix} 1 \\ 8 \\ 27 \\ 64 \\ 125 \\ 216 \\ 343 \\ 512 \\ 729 \\ 1000 \end{matrix}$

6. $40v^3 - 625$
 $5(8v^3 - 125)$
 $5(2v - 5)(4v^2 + 10v + 25)$

15.
$$\begin{array}{r|rrrr} 4 & 1 & -4 & 0 & 8 & -32 \\ & & 4 & 0 & 0 & 32 \\ \hline & 1 & 0 & 0 & 8 & 0 \end{array}$$

 $x^3 + 8$
 $(x+2)(x^2 - 2x + 4)(x-4)$

11. $(5p+1)(5p-1)(p-1)$

12. $(m+2)(3m+2)(3m-2)$

15. $x^4 + x^2 - 20$
 $(x^2 - 4)(x^2 + 5)$
 $(x+2)(x-2)(x^2 + 5)$

16. $6y^4 - 5\sqrt{y^3} - 4$
 $(\quad)(\quad)$
 $6y^3 + 3y^3 - 8y^3 - 4$
 $3y^3(2y^3 + 1) - 4(2y^3 + 1)$
 $(3y^3 - 4)(2y^3 + 1)$

21. $-2(2x^2 - 3)(x^2 - 5)$

22. $2(b-2)(b^2 + 2b + 4)(b+7)$
 $2b^4 + 14b^3 - 16b - 112$
 $2b^3(b+7) - 16(b+7)$
 $(2b^3 - 16)(b+7)$
 $2(b^3 - 8)(b+7)$
 $2(b-2)(b^2 + 2b + 4)(b+7)$

13. $(x^2 + 9)(x+3)(x-3)$

14. $(2x^2 + 3)(x^2 + 1)$

16. $6x^4 - 9x^2 + 3$
 $3(2x^4 - 3x^2 + 1)$
 $3(2x - 1)(x - 1)$

15. $(a^2b + 5)(a^4b^2 - 5a^2b + 25)$

16. $2ac^2 - 5bc^2 - 2ad^2 + 5bd^2$
 $c^2(2a - 5b) - d^2(2a - 5b)$
 $(2a - 5b)(c^2 - d^2)$
 $(2a - 5b)(c+d)(c-d)$

15. $a^4b^3 + 125$
 $(a^2b + 5)(a^4b^2 - 5a^2b + 25)$
 $a^2b \cdot a^2b = a^4b^2$
 $a^2 \cdot 5 = 5a^2$
 $5 \cdot 5 = 25$

13. $x^2 + 3x + c$
 $(x + \frac{3}{2})^2$
 $c = \frac{9}{4}$

$$15. 4x^7 - 64x^3$$

$$4x^3(x^4 - 16)$$

$$4x^3(x^2 + 4)(x^2 - 4)$$

$$4x^3(x^2 + 4)(x + 2)(x - 2)$$

14.

$$14. 5x^2 - \underline{20x} - 25$$

$$(5x - 5)(x + 5)$$

$-5x$

$25x$

$$5(x^2 - 4x - 5)$$

$$5(x + 1)(x - 5)$$

GCF

2 terms:

$$a^2 - b^2 = (a+b)(a-b)$$

$$a^3 \pm b^3 = (a+b)(a^2 - ab + b^2)$$

3 terms: - guess-check ✓
 - product ac w/ grouping ✓

$$\left(\quad \right) \left(\quad \right)$$

$$* \text{PS} : a^2 + 2ab + b^2 = (a+b)^2$$

4 or more terms:
 Grouping

* if factor is given, may use
 synthetic division

$$x^2 + bx + c = \left(x + \frac{b}{2}\right)^2$$

$$c = \left(\frac{b}{2}\right)^2$$

$$5x^2 - 20x - 25 = 5(x^2 - 4x - 5)$$

$$= 5(x+1)(x-5)$$

$$= (5x-5)(x+5)$$

$$+25x$$

$$4x^7 - 64x^3$$

$$4x^3(x^4 - 16)$$

$$4x^3(x^2 - 4)(x^2 + 4)$$

$$4x^3(x+2)(x-2)(x^2 + 4)$$